

---

# Simple is Better: Training an End-to-end Contract Bridge Bidding Agent without Human Knowledge

---

Qucheng Gong<sup>1</sup> Tina Jiang<sup>1</sup> Yuandong Tian<sup>1</sup>

## Abstract

Contract bridge is a multi-player imperfect-information game where one partnership collaborate with each other to compete against the other partnership. The game consists of two phases: bidding and playing. While playing is relatively easy for modern software, bidding is challenging and requires agents to learn a communication protocol to reach the optimal contract jointly, with their own private information. The agents need to exchange information to their partners, and interfere opponents, through a sequence of actions. In this work, we train a strong agent to bid competitive bridge purely through selfplay, outperforming WBridge5, a championship-winning software. Furthermore, we show that explicitly modeling belief is not necessary in boosting the performance. To our knowledge, this is the first competitive bridge agent that is trained with no domain knowledge. It outperforms previous state-of-the-art that use human replays with 70x fewer number of parameters.

## 1. Introduction

Games have long been recognized as a testbed for reinforcement learning. Recent technology advancements have outperformed top level experts in perfect information games like Chess (9) and Go (18; 20), through human supervision and selfplay. During recent years researchers have also steered towards imperfect information games, such as Poker (8; 16), Dota 2 (3), and real-time strategy games (5; 22). There are multiple programs which focus specifically in card games. Libratus (8) and DeepStack (16) outperforms human experts in two-player Texas Holdem. Bayesian Action Decoder (11) is able to achieve near optimal performance in multi-player collaborative games like Hanabi.

---

\*Equal contribution <sup>1</sup>Facebook AI Research, Menlo Park, California, USA. Correspondence to: Yuandong Tian <yuan-dong@fb.com>.

Contract Bridge, or simply Bridge, is a trick-taking card game with 2 teams, each with 2 players. There are 52 cards (4 suits, each with 13 cards). Each player is dealt with 13 cards. The game has two phases: bidding and playing. In the bidding phase, each player can only see their own card and negotiate in turns via proposing *contract*, which sets an explicit goal to aim at during the playing stage. High contracts override low ones. Players with stronger cards aim at high contracts for high reward; while failing to reach the contract, the opponent team receives rewards. Therefore, players utilize the bidding phase to reason about their teammate and opponents' cards for a better final contract. In the playing phase, one player reveals their cards publicly. In each round, each player plays one card in turn and the player with best card wins the round. The score is simply how many rounds each team can win. We introduce the game in more details in Appendix A.

Historically AI programs can handle the playing phase well. Back in 1999, the GIB program (12) placed 12th among 34 human experts partnership, in a competition without the bidding phase. In more recent years, Jack (2) and Wbridge5 (4), champions of computer bridge tournament, has demonstrated strong performances against top level professional humans.

On the other hand, the bidding phase is very challenging for computer programs. During the bidding phase a player can only access his own 13 cards (private information) and the bidding history (public information). They need to exchange information with their partners and try to interfere opponents from doing so through a sequences of non-decreasing bids. Moreover these bids also carry the meaning of suggesting a contract. If the bid surpasses the highest contract they can make, they will get negative score and risk of being doubled. Thus, the amount of information exchange is constrained and dependent on the actual hands. Nevertheless the state space is very large. A player can hold  $6.35 \times 10^{11}$  unique hands and there are  $10^{47}$  possible bidding sequences. Human has designed a lot of hand-crafted rules and heuristics to cover these cases, called bidding system, and designated a meaning to many common bidding sequences. However, due to large state space, the meaning of these sequences are sometimes ambiguous or conflicting. The bidding system

itself also has room for improvement. The award winning programs often implement a subset of some specified human bidding system. Recently, there are also attempts to learn such a bidding system automatically through reinforcement learning. These methods either focus on bidding in the collaborative only setting, where both opponents will bid PASS throughout (23; 24), or heavily used human expert data for extra supervision (17).

In this work, we propose a system that is the state-of-the-art in competitive bridge bidding. It allows end-to-end training without any human knowledge through selfplay. We propose a novel bidding history representation, and remove any explicit modeling of belief in other agent’s state, which are shown to be critical in previous works (17; 23). We show that selfplay schedule and details are critical in learning imperfect information games. We use a much smaller model (about 1/70 in total parameters compared with previous state-of-the-art (17)), and reach better performance than the baselines (17; 24). Furthermore, we outperform world computer bridge championship Wbridge5 (4) by 0.41 IMPs per board over a tournament of 64 boards. Finally, we show an interpretation of the trained system, and will open source the code, model, and experimental data we use.

## 2. Related work

Imperfect information games, especially card games, have drawn multiple researchers’ attention. Prior works on two-player Texas Holdem mainly focus on finding the Nash Equilibrium through variations of counterfactual regret minimization (25). Libratus (8) utilizes nested safe subgame solving and handles off-tree actions by real time computing. It also has a built-in self improver to enhance the background blueprint strategy. DeepStack (16) proposed to use a value network to approximate the value function of the state. They both outperform top human experts in the field. Bayesian Action Decoder (BAD)(11) proposes to model public belief and private belief separately, and sample policy based on an evolving deterministic communication protocol. This protocol is then improved through Bayesian updates. BAD is able to reach near optimal results in two-player Hanabi, outperforming previous methods by a significant margin.

In recent years there are also multiple works specifically focusing on contract bridge. Yeh and Lin (24) uses deep reinforcement learning to train a bidding model in the collaborative setting. It proposes Penetrative Bellman’s Equation (PBE) to make the Q-function updates more efficient. The limitation is that PBE can only handle fixed number of bids, which are not realistic in a normal bridge game setting. We refer to this approach as `baseline16`. Tian et al (23) proposes Policy Belief Learning (PBL) to alternate training between policy learning and belief learning over the whole selfplay process. PBL also only works on the col-

laborative setting. Rong et al (17) proposes two networks, Estimation Neural Network (ENN) and Policy Neural Network (PNN) to train a competitive bridge model. ENN is first trained supervisedly from human expert data, and PNN is then learned based on ENN. After learning PNN and ENN from human expert data, the two network are further trained jointly through reinforcement learning and selfplay. PBE claims to be better than Wbridge5 in the collaborative setting, while PNN and ENN outperforms Wbridge5 in the competitive setting. We refer to this approach as `baseline19`.

Selfplay methods have been proposed for a long time. Back in 1951, Brown et al (7) proposes fictitious play in imperfect information games to find the Nash Equilibrium. This is a classic selfplay algorithm in game theory and inspires many extensions and applications (8; 13; 14; 16). Large scale selfplay algorithms do not emerge until recent years, partially due to computation constraint. AlphaGo (18) uses selfplay to train a value network to defeat the human Go champion Lee Sedol 4:1. AlphaGoZero (20) and AlphaZero (19) completely discard human knowledge and train superhuman models from scratch. In Dota 2 and StarCraft, selfplay is also used extensively to train models to outperform professional players.

Belief modeling is also very critical in previous works about imperfect information games. Besides the previous mentioned card game agents (11; 17; 23), LOLA agents (10) are trained with anticipated learning of other agents. StarCraft Defogger (21) also tries to reason about states of unknown territory in real time strategy games.

## 3. Method

### 3.1. Problem Setup

We focus on the bidding part of the bridge game. Double Dummy Solver (DDS) (1) computes the maximum tricks each side can get during the playing phase if all the plays are optimal. Previous works show that DDS is a good approximate to human expert real plays (17), so we directly use the results of DDS at the end of bidding phase to assign reward to each side. The training dataset contains randomly generated 2.5 million hands along with their precomputed DDS results. The evaluation dataset contains 100k such hands. We will open source this data for the community and future work.

Inspired by the format of duplicate bridge tournament, during training and evaluation, each hand is played twice, where a specific partnership sits North-South in one game, and East-West in another. The difference in the results of the two tables is the final reward. In this way, the impact of randomness in the hands is reduced to minimum and model’s true strength can be better evaluated. The difference in

Own Cards	Bid history, multi-hot of contract bids					Vulnerability	Available Action
	Own	Partner	Left Opp	Right Opp	Double Indicator		
52	35	35	35	35	35	2	38

W	N	E	S
1♣	X	1♥	
1♠	2♣	P	?

Figure 1. Input representation. With the decision point shown in the example, South will mark the following bits in the bidding history encoding: 1♥ in "Own" segment, 1♣ and 2♣ in "Partner" segment, 1♠ in "Left Opp" segment, and 1♣ in "Double Indicator" segment.

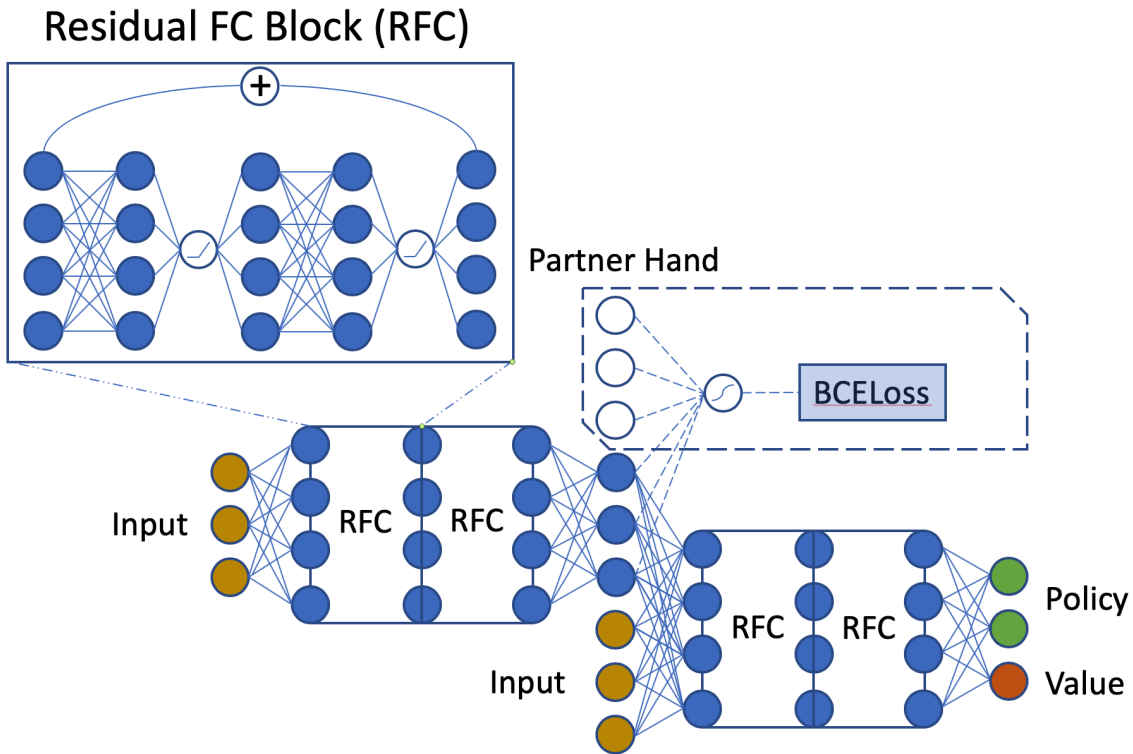


Figure 2. Network Architecture. Supervision from partner’s hand is unused in the main results, and used in the ablation studies.

scores is then converted to IMPs scale, and then normalized to [-1, 1].

### 3.2. Input Representation

We encode the state of a bridge game to a 267 bit vector. The first 52 bits indicate that if the current player holds a specific card. The next 175 bits encodes the bidding history, which consists of 5 segments of 35 bits each. These 35 bit segments correspond to 35 contract bids. The first segment indicates if the current player has made a corresponding bid in the bidding history. Similarly, the next 3 segments encodes the contract bid history of the current player’s partner, left opponent and right opponent. The last segment indicates that if a corresponding contract bid has been doubled or redoubled. Since the bidding sequence can only be non-

decreasing, the order of these bids are implicitly conveyed. The next 2 bits encode the current vulnerability of the game, corresponding to the vulnerability of North-South and East-West respectively. Finally, the last 38 bits indicates whether an action is legal, given the current bidding history.

We emphasize that this encoding is quite general and there is not much domain-specific information. `baseline19` presents a novel bidding history representation using positions in the maximal possible bidding sequence, which is highly specific to the contract bridge game.

### 3.3. Network

We use a similar network structure that is used in `baseline19`. As show in Figure 2 The network consists of an initial fully connected layer, then 4 fully connected

layer with skip connections added every 2 layers to get a latent representation. We use 200 neurons at each hidden layer, hence it is much smaller (about 1/70 in parameter size compared with `baseline19`). The full network architecture is shown In Figure 2. However, during our training we do not use partner’s information to further supervise the belief training. We investigate the impact of training belief separately, and find that our model cannot benefit from extra supervision from partner’s information.

From the latent representation, one branch is to a policy head. It is a fully connected layer to 38 output neurons, masking out illegal actions provided in the input, and then normalizes to a log policy. The other branch is a value head, which is just a fully connected layer to 1 neuron.

### 3.4. Training Details

**RL Method.** We use selfplay on random data to train our models. The model is trained with A3C (15) using improved ELF framework (22). ELF supports off-policy training with importance factor correction, and has inherent parallelization implementations to make training fast. The whole training process takes roughly 4-5 hours to converge on a single GPU.

**Training Parameters.** During training we run 500 games in parallel and use batch size of 100. We use an entropy ratio of 0.01 in A3C training. The discount factor is set to 1 to encourage longer sequences of information exchange, and since the bidding is non-decreasing, it will not cause convergence issue. We train the model using RMSProp with a learning rate of 1e-3. We fine tune our model by dropping learning rate to 1e-4 at 50k training minibatches and further dropping it to 1e-5 at 70k minibatches. We use multinomial exploration to get the action from a policy distribution.

**Baselines.** As suggested by the authors of `baseline16`, we modify their pretrained model to bid competitively, by bidding PASS if the cost of all bids are greater than 0.2. We implement this and further fix its weakness that the model sometimes behaves randomly in a competitive setting if the scenario can never occur in the collaborative setting. We benchmark against them at each episode. We could not fully reproduce the results in `baseline19` so we cannot directly compare against them.

## 4. Experiments

### 4.1. Main Results

We train a competitive bridge bidding model through self-play. We perform a grid search on hyper-parameters such as discount factor, exploring rate, learning schedules and find the best combination. The training curve against

`baseline16` is shown in Figure 3. As can be seen, we significantly beat `baseline16` 2.31 IMPs per board. We manually run a 64 board tournament against `Wbridge5`, and outperforms it by 0.41 IMPs per board. This also surpasses the previous state-of-the-art `baseline19`, which outperforms `Wbridge5` by 0.25 IMPs per board. It is shown in previous work that a margin of 0.1 IMPs per board is significant (17).

We outperform `baseline16` with a large margin partially due to `baseline16` cannot adapt well to competitive bidding setting. It can also only handle a fixed length of bids. We outperform `baseline19` mainly due to a better history encoding and not to model belief explicitly. These results are shown in the ablation studies. We also show an interpretation of the learned bidding system of our model, shown in Appendix B.

### 4.2. Ablation Studies

Prior works focus on explicitly modeling belief, either by adding an auxiliary loss to train jointly (17), or alternating stages between training policy and belief (23). However, training belief using supervision from partner’s hand does not help in our model. We set the final loss as  $L = rL_{belief} + L_{A3C}$ . where  $r$  is a hyper-parameter to control the weight on the auxiliary task, As shown in Table 1, when  $r = 0$ , the model reaches the best performance and the performance decreases as  $r$  increase. This demonstrates that focusing on the main task can achieve better results.

Bidding history encoding plays a critical role in model architecture. `baseline19` proposed a novel representation of sequenced bidding history, which listed all possible actions in a sequence and then labeled what has been used. We compared our representation to theirs. As shown in Table 1 our encoding can reach a better performance. The potential reason why our encoding performs better is that the intrinsic order of bridge bidding is already kept by the action itself, so there is no need to specify the sequence, and our encoding captures the owner of each action.

In imperfect information games, one common strategy is to use a pool of opponents to add diversity to the experiences. We also investigate this strategy in bridge. To increase the diversity, we set two ways: First, we maintain a model-zoo with 20 most recent models and then randomly sample the opponent model from this zoo; Second, we save the 20 models with best performance and sample using the Nash Averaging strategy (6). We find self-play with opponent using the most recent model works best in terms of performance comparing to baseline models as shown in Table 1. One possible explanation is that bridge is a game with both competition and collaborations. Mixed strategy can mislead both opponents and partners, so a Nash Averaging strategy will not work well enough. Hence, using the most recent

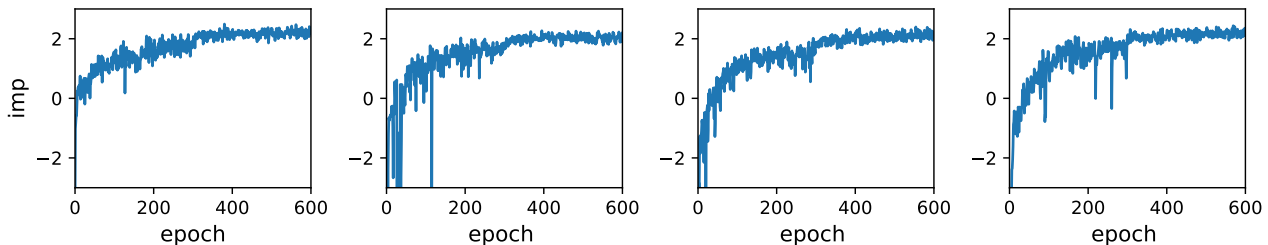


Figure 3. Training curves for different update frequency. From left to right, the opponent model is updated every 1, 50, 100, 200 minibatches. Epoch is defined as 200 minibatches.

Table 1. Performance Comparison. The left table compares performance when giving different weights to the belief loss and the performance when using the same history encoding as (17). The right table shows performance under different level of diversity of opponent models, by updating the opponent model at different frequency or sample opponent model randomly or using Nash Equilibrium.

A		B	
Ratio r	imps $\pm$ std	Update frequency	imps $\pm$ std
0	<b>2.31 <math>\pm</math> 0.15</b>	1	2.26 $\pm$ 0.10
0.01	1.90 $\pm$ 0.29	50	2.14 $\pm$ 0.20
0.1	1.63 $\pm$ 0.27	100	2.08 $\pm$ 0.07
1	1.22 $\pm$ 0.22	200	<b>2.31 <math>\pm</math> 0.15</b>
Hist encoding		Opponent Diversity	
baseline19 hist	1.27 $\pm$ 0.22	Randomly sample	2.09 $\pm$ 0.04
		Nash averaging	2.18 $\pm$ 0.20

model is more suitable for such training.

Besides the strategy to choose opponent model, we also study the impact of opponent model update frequency. As can be seen from Table 1, the final performances are similar. However, the training curve Figure 3 shows different patterns. Using the exact the same model for selfplay opponent during the training shows the most stable results, especially at the early stage of the training. It is possibly due to the fast model progression during the early stage of the training. If selfplay opponent does not update frequent enough it cannot learn new knowledge.

## 5. Conclusion and Future Work

In conclusion, we provide a strong baseline that is the state-of-the-art in bridge bidding, with a significantly smaller model. We offer insights through ablation studies to rethink about the training process and belief modeling in imperfect information games. We also interpret the learned bidding system through statistical visualizations and bidding examples. Our code, model and experimental data will be publicly available. We believe this addition is beneficial to

the bridge community and imperfect information game researchers, to push forward further research in this direction. It remains a challenging problem to correctly model belief, to reason counterfactually, and to communicate efficiently in multi-agent imperfect information games. We leave this as future work.

## References

- [1] Double dummy solver. <https://github.com/dds-bridge/dds>. Accessed: 2019-05-22.
- [2] Jack bridge. <http://www.jackbridge.com/eindex.htm>. Accessed: 2019-05-22.
- [3] Openai5. <https://openai.com/blog/openai-five/>. Accessed: 2019-05-22.
- [4] Wbridge5. <http://www.wbridge5.com/>. Accessed: 2019-05-22.
- [5] Kai Arulkumaran, Antoine Cully, and Julian Togelius. Alphastar: An evolutionary computation perspective. *CoRR*, abs/1902.01724, 2019.

- [6] David Balduzzi, Karl Tuyls, Julien Pérolat, and Thore Graepel. Re-evaluating evaluation. *CoRR*, abs/1806.02643, 2018.
- [7] GW Brown. Iterative solution of games by fictitious play, in “activity analysis of production and allocation”(tc koopmans, ed.), 1951.
- [8] Noam Brown and Tuomas Sandholm. Superhuman ai for heads-up no-limit poker: Libratus beats top professionals. *Science*, 359(6374):418–424, 2018.
- [9] Murray Campbell, A Joseph Hoane Jr, and Feng-hsiung Hsu. Deep blue. *Artificial intelligence*, 134(1-2):57–83, 2002.
- [10] Jakob Foerster, Richard Y Chen, Maruan Al-Shedivat, Shimon Whiteson, Pieter Abbeel, and Igor Mordatch. Learning with opponent-learning awareness. In *Proceedings of the 17th International Conference on Autonomous Agents and MultiAgent Systems*, pages 122–130. International Foundation for Autonomous Agents and Multiagent Systems, 2018.
- [11] Jakob N. Foerster, Francis Song, Edward Hughes, Neil Burch, Iain Dunning, Shimon Whiteson, Matthew Botvinick, and Michael Bowling. Bayesian action decoder for deep multi-agent reinforcement learning. *CoRR*, abs/1811.01458, 2018.
- [12] Matthew L Ginsberg. Gib: Steps toward an expert-level bridge-playing program. In *IJCAI*, pages 584–593. Citeseer, 1999.
- [13] Johannes Heinrich, Marc Lanctot, and David Silver. Fictitious self-play in extensive-form games. In *International Conference on Machine Learning*, pages 805–813, 2015.
- [14] Johannes Heinrich and David Silver. Deep reinforcement learning from self-play in imperfect-information games. *arXiv preprint arXiv:1603.01121*, 2016.
- [15] Volodymyr Mnih, Adria Puigdomenech Badia, Mehdi Mirza, Alex Graves, Timothy Lillicrap, Tim Harley, David Silver, and Koray Kavukcuoglu. Asynchronous methods for deep reinforcement learning. In *International conference on machine learning*, pages 1928–1937, 2016.
- [16] Matej Moravčík, Martin Schmid, Neil Burch, Viliam Lisý, Dustin Morrill, Nolan Bard, Trevor Davis, Kevin Waugh, Michael Johanson, and Michael Bowling. Deepstack: Expert-level artificial intelligence in heads-up no-limit poker. *Science*, 356(6337):508–513, 2017.
- [17] Jiang Rong, Tao Qin, and Bo An. Competitive bridge bidding with deep neural networks. *CoRR*, abs/1903.00900, 2019.
- [18] David Silver, Aja Huang, Chris J Maddison, Arthur Guez, Laurent Sifre, George Van Den Driessche, Julian Schrittwieser, Ioannis Antonoglou, Veda Panneershelvam, Marc Lanctot, et al. Mastering the game of go with deep neural networks and tree search. *nature*, 529(7587):484, 2016.
- [19] David Silver, Thomas Hubert, Julian Schrittwieser, Ioannis Antonoglou, Matthew Lai, Arthur Guez, Marc Lanctot, Laurent Sifre, Dhharshan Kumaran, Thore Graepel, Timothy Lillicrap, Karen Simonyan, and Demis Hassabis. A general reinforcement learning algorithm that masters chess, shogi, and go through self-play. *Science*, 362(6419):1140–1144, 2018.
- [20] David Silver, Julian Schrittwieser, Karen Simonyan, Ioannis Antonoglou, Aja Huang, Arthur Guez, Thomas Hubert, Lucas Baker, Matthew Lai, Adrian Bolton, et al. Mastering the game of go without human knowledge. *Nature*, 550(7676):354, 2017.
- [21] Gabriel Synnaeve, Zeming Lin, Jonas Gehring, Dan Gant, Vegard Mella, Vasil Khalidov, Nicolas Carion, and Nicolas Usunier. Forward modeling for partial observation strategy games—a starcraft defogger. In *Advances in Neural Information Processing Systems*, pages 10738–10748, 2018.
- [22] Yuandong Tian, Qucheng Gong, Wenling Shang, Yuxin Wu, and C. Lawrence Zitnick. ELF: an extensive, lightweight and flexible research platform for real-time strategy games. In *Advances in Neural Information Processing Systems 30: Annual Conference on Neural Information Processing Systems 2017, 4-9 December 2017, Long Beach, CA, USA*, pages 2656–2666, 2017.
- [23] Zheng Tian, Shihao Zou, Tim Warr, Lisheng Wu, and Jun Wang. Learning multi-agent implicit communication through actions: A case study in contract bridge, a collaborative imperfect-information game. *CoRR*, abs/1810.04444, 2018.
- [24] Chih-Kuan Yeh and Hsuan-Tien Lin. Automatic bridge bidding using deep reinforcement learning. *CoRR*, abs/1607.03290, 2016.
- [25] Martin Zinkevich, Michael Johanson, Michael Bowling, and Carmelo Piccione. Regret minimization in games with incomplete information. In *Advances in neural information processing systems*, pages 1729–1736, 2008.

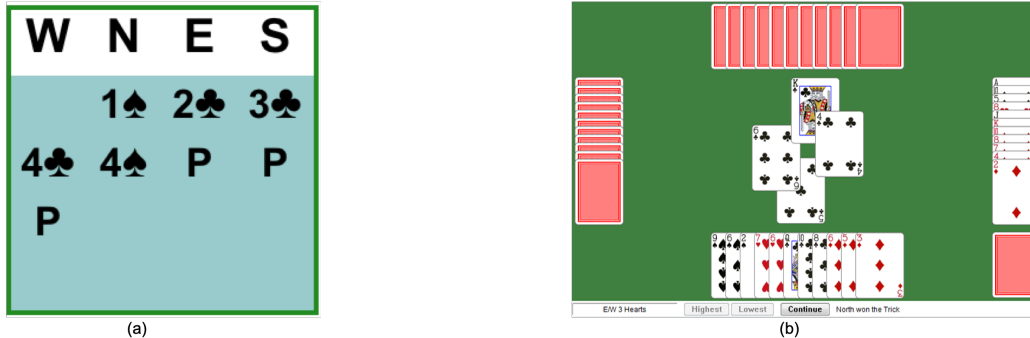


Figure 4. (a) A bidding example. North-South prevail and will declare the contract 4♠. During the bidding, assuming natural bidding system, the bid 1♠, 2♣, 4♣ and 4♠ are natural bids, which shows lengths in the nominated suit. The bid 3♣ is an artificial bid, which shows a good hand with ♠ support for partner, and shows nothing about the ♣ suit. To make the contract, North-South needs to take 10 tricks during the playing phase. (b) A playing example. Currently shown is the 2nd round of the playing phase. The dummy’s card is visible to all players, and controlled by his partner, declarer. In the current round North player wins with ♣K, and will lead the next round.

## A. The Bridge Game

Bridge is played with a standard 52-card deck, and each player is dealt with 13 cards. There are two phases during the game, namely **bidding** and **playing**. After the game, **scoring** is done based on the bidding and playing. An example of contract bridge bidding and playing is shown in Figure 4.

**Bidding phase.** During the bidding phase, each player takes turns to bid from 38 available actions. The sequence of bids form an auction. There are 35 contract bids, which consists of a level and a strain, ranging from an ordered set {1♣, 1♦, 1♥, 1♠, 1NT, 2♣, ..7NT} where NT stands for No-Trump. The level determines the number of tricks needed to make the contract, and the strain determines the trump suit if the player wins the contract. Each contract bid must be either higher in level or higher in strain than the previous contract bids. There are also 3 special bids. Pass (P) is always available when a player is not willing to make a contract bid. Three consecutive passes will terminate the auction (Four if the consecutive passes happen in the beginning of the auction), and the last contract bid becomes the final contract, with their side winning the contract. Double (X) can be used when either opponent has made a contract bid. It will increase both the contract score and the penalty score for not making the contract. Originally this is used when a player has high confidence that opponent’s contract cannot be made, but it can also be used to communicate other information. Finally, Redouble (XX) can be used to further amplify the risk and reward of a contract, if the contract is doubled. Similarly, this bid can also be used to convey other information.

**Playing phase.** After the bidding phase is over, the contract is determined, and the owner of the final contract is the declarer. His partner becomes dummy. The other partnership

is the defending side. During the playing phase, there are 13 rounds and each round the player plays a card. The first round is started with the defending side, and then dummy immediately lays down his cards, and declarer can control both him and dummy. The trump suit is designated by the strain of the final contract (Or None if the strain is NT). Each round, every player has to follow suit. If a player is out of a certain suit, he can play a trump card to beat it. Discarding other suits is always losing in this round. The player with the best card wins a trick, and will play first in the next round. The required number of tricks to make the contract is contract level + 6. At the end of the game, if the declaring side wins enough tricks, they make the contract. Tricks in addition to the required tricks are called over-tricks. If they fail to make the contract, the tricks short are called under-tricks.

**Scoring.** if the contract is made, the declaring side will receive contract score as a reward, plus small bonuses for over-tricks. Otherwise they will receive negative score determined by under-tricks. Contracts below 4♥ (except 3NT) are called **part score contracts**, with relatively low contract scores. Contracts 4♥ and higher, along with 3NT, are called **game contracts** with a large bonus score. Finally, Contract with level 6 and 7 are called **small slams** and **grand slams** respectively, each with a huge bonus score if made. To introduce more variance, a vulnerability to randomly assigned to each board to increase both these bonuses and penalties for failed contracts. After a raw score is assigned it is usually converted to IMPs scale <sup>1</sup> in a tournament match setting, which is roughly proportional to the square root of the raw score, and ranges from 0 to 24.

<sup>1</sup>[https://www.acbl.org/learn\\_page/howtoplaybridge/howto-keepscore/duplicate/](https://www.acbl.org/learn_page/howtoplaybridge/howto-keepscore/duplicate/)

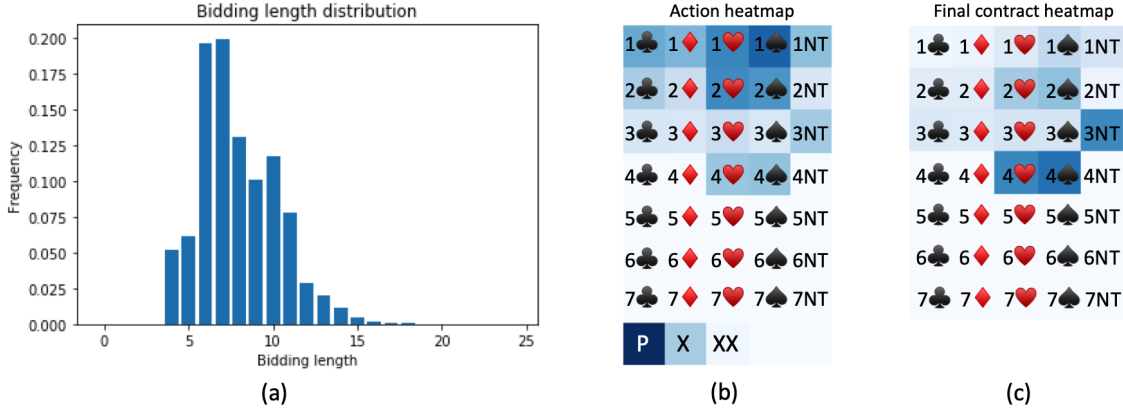


Figure 5. Statistical visualization. (a) Bidding length histogram. (b) Heatmap for all actions during the bidding. (c) Heatmap for final contracts reached.

## B. Interpretation

### B.1. Visualization

It is interesting to visualize what the model has learned, and understand some rational behind the learned conventions. In Figure 5, we show the bidding length distribution and frequency of each bid used, as well as the distribution of final contracts. The results are averaged from our best 3 models. We can see that typically agents exchanges 6-10 rounds of information to reach the final contract. The agent uses low level bids more frequently and puts an emphasis on ♠ and ♣ contracts. The final contract is mostly part scores and game contracts, particularly often 3NT, 4♥, 4♠, and we observe very few slam contracts. This is because part scores and game contracts are optimal based on DDS for 87% of hands<sup>2</sup>. The model does not optimize to bid slam contracts, because it needs to hold a firm belief after longer rounds of information exchange to bid a slam contract, and the risk of not making the contract is very high.

### B.2. Opening Table

There are two mainstream bidding system human experts use. One is called natural, where opening and subsequent bids usually shows length in the nominated suit, e.g. the opening bid 1♥ usually shows 5 or more ♥ with a decent strength. The other is called precision, which heavily relies on relays of bids to partition the state space, either in suit lengths or hand strengths. e.g. an opening bid of 1♣ usually shows 16 or more High Card Points (HCP)<sup>3</sup>, and a subsequent 1♥ can show 5 or more ♠. To further understand the bidding system the model learns, it is interesting to establish an opening table of the model, defined by the meaning of each opening bid. We select one of the best models,

<sup>2</sup> <https://lajollabridge.com/Articles/PartialGameSlamGrand.htm>

<sup>3</sup>High Card Points is a heuristic to evaluate hand strength, which counts A=4, K=3, Q=2, J=1

Table 2. Opening table comparisons. “bal” is abbreviation for a balanced distribution for each suit.

opening bids	ours	SAYC
1♣	8-20 HCP	12+ HCP, 3+♣
1♦	8-18 HCP, 4+♦	12+ HCP, 3+♦
1♥	8-18 HCP, 4-6♥	12+ HCP, 5+♥
1♠	7-16 HCP, 4-6♠	12+ HCP, 5+♠
1NT	14-18 HCP, bal	15-17 HCP, bal
2♣	8-13 HCP, 5+♣	22+ HCP
2♦	7-11 HCP, 5+♦	5-11 HCP, 6+♦
2♥	7-11 HCP, 5+♥	5-11 HCP, 6+♥
2♠	7-11 HCP, 5+♠	5-11 HCP, 6+♠
2NT	14+ HCP, 4+♣, 4+♦	20-21 HCP, bal

and check the length of each suit and HCP associated with each opening bid. From the opening table, it appears that the model learns a semi-natural bidding system with very aggressive openings.

### B.3. Bidding Examples

We check a few interesting hands from the tournament between our model and Wbridge5. We present the following 5 examples in Figure 6.

(a) This is a purely collaborative auction where our agents sit North-South. South chooses to open an artificial short ♣ suit. North shows his ♥ suit, and South raises his partner in return. With a strong hold North re-raise to 4♥, a game contract. The best contract determined by double dummy solver is 6♥, but it is due to the favorable position of ♥K, so it is not worth the risk to bid it.

(b) This is a competitive auction where our agents sit East-West. The first few bids are natural. East, holding 5 cards in both ♥ and ♠, takes action to double opponent’s 1NT bid. While partner is silent East balances with 2♠ bid again.



## Simple is Better: Training an End-to-end Contract Bridge Bidding Agent without Human Knowledge

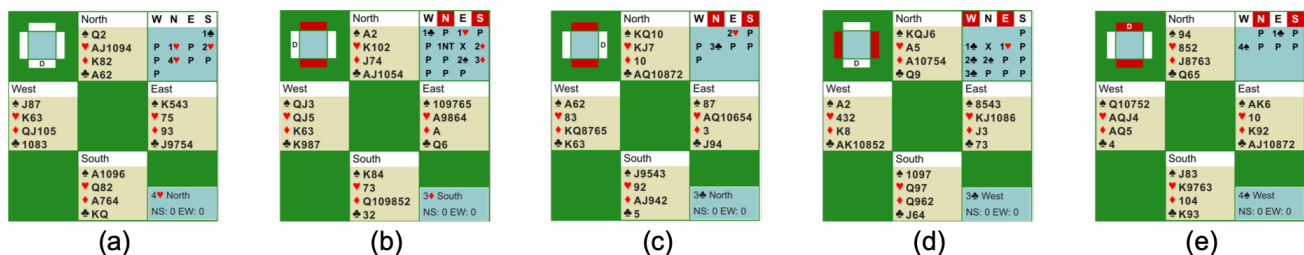


Figure 6. Bidding examples. D marks the dealer, and red seats indicate vulnerable side.

This successfully pushes opponents into a non-making  $3\heartsuit$  contract.

(c) Preemptive bids play an important role in bridge bidding. Historically a 2 level opening indicates a very strong hand, but modern bidding system bids it with a relative weak hand with a long suit (called weak 2). It is due to this hand type is much more frequent, and it can disrupt opponent's bidding by taking away the bidding space. In a standard system weak 2 usually promises 6 cards in the nominated suit, but from the opening table we can see that our agents do it more aggressively with routinely 5 cards. In this hand our agent opens a weak  $2\heartsuit$ , and as a result North-South fails to find their best contract in  $\heartsuit$ , and bids a non-making  $3\clubsuit$  instead, due to lack of information exchange.

(d) Double is a critical bid, unique to competitive bidding. The original meaning is that the doubler is confident to beat opponents' contract. However it can also be used to transmit other information. In this hand, our agent sitting North doubles opponent's  $1\clubsuit$  with a short  $\clubsuit$  suit and support for other suits, and a strong hand. This aligns well with the meaning of a modern "technical double".

(e) The model jumps to  $4\spadesuit$  too quickly. While the contract is making, it fails to investigate slam opportunities on this hand.