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Stock time series pattern matching: Template-based vs. rule-based approaches

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Abstract

One of the major duties of financial analysts is technical analysis. It is necessary to locate the technical patterns in the stock price movement charts to analyze the market behavior. Indeed, there are two main problems: how to define those preferred patterns (technical patterns) for query and how to match the defined pattern templates in different resolutions. As we can see, defining the similarity between time series (or time series subsequences) is of fundamental importance. By identifying the perceptually important points (PIPs) directly from the time domain, time series and templates of different lengths can be compared. Three ways of distance measure, including Euclidean distance (PIP-ED), perpendicular distance (PIP-PD) and vertical distance (PIP-VD), for PIP identification are compared in this paper. After the PIP identification process, both template- and rule-based pattern-matching approaches are introduced. The proposed methods are distinctive in their intuitiveness, making them particularly user friendly to ordinary data analysts like stock market investors. As demonstrated by the experiments, the template- and the rule-based time series matching and subsequence searching approaches provide different directions to achieve the goal of pattern identification. © 2006 Elsevier Ltd. All rights reserved.

Keywords: Stock time series; Technical pattern; Whole series pattern matching; Subsequence pattern matching; Perceptually important point identification

1. Introduction

A time series is a collection of observations chronologically made. Time series data can be easily obtained from various domains such as scientific, medical and financial applications, e.g. daily temperatures, daily sales totals, and prices of mutual funds and stocks. The time series data has the nature of includes: large data size and high dimensionality. Therefore, researchers have been interested in finding similar time series (Das et al., 1997) and querying time series database (Agrawal et al., 1993). Thus, defining the similarity between time series (or time series segments) is of fundamental importance. Abundant algorithms are existed for measuring similarity between time series measuring the Euclidean distance (ED).

Indeed, a large amount of time series data is from the stock market. Stock time series has its own characteristics over other time series data like electrocardiogram (ECG). For example, technical analysis is usually used to identify patterns of market behavior, which have a high probability to repeat themselves. These patterns are similar in the overall shape but with different amplitudes and/or durations. Moreover, these patterns can be characterized by a few data points. For example, Fig. 1 shows the time series patterns that belong to the same technical pattern (i.e. head-and-shoulder pattern) but with different outlooks. Although these patterns may have a large ED, they should also be strictly considered as similar.

In this paper, a flexible time series pattern matching scheme that is customized to handle stock time series patterns is introduced. Emphasis of this work is on stock pattern matching and is generally referred to the technical (analysis) patterns, such as head-and-shoulder or double tops patterns. The proposed scheme adopts the time

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Fig. 1. Head-and-shoulder time series patterns.

domain approach, which is more intuitive to stock market analysts since those critical points will not be smoothed out as in other domains after transformation. It is able to carry out matching between time series (or time series segments) and query patterns of different lengths effectively and efficiently. The approach will be explained with two sample queries. Considering stock time series, one may expect having queries like: Q1:*Find all stocks which behave "similarly" to stock A*.

Q2:Find all 1-week "head-and-shoulder" patterns in the closing prices of a high-tech stock.

The query results are expected to provide useful information for different stock analysis activities. Q1 is a whole time series matching process and it can be considered as follows. Given a query sequence $Q = (q_1, ..., q_n)$ and a set of data sequences $P = (p_1, ..., p_m)$ extracted from a dataset, we want to identify a set of P that is similar to Q.

As for queries like Q2 in fact, are tightly coupled with the patterns frequently used in technical analysis, e.g. headand-shoulder, double tops, triple tops, spike top, rounded top, and it is a subsequence pattern-matching process. We have a query sequence $Q = (q_1, ..., q_n)$ and a longer sequence $P = (p_1, ..., p_m)$. The task is to find all the subsequences $S = (s_1, ..., s_w)$ in P, which match Q and w < <m. Subsequence matching requires that the query Q be placed at every possible offset. The sliding window is commonly used, m-w+1 subsequences will be searched and those fulfill the pattern-matching criteria will be located.

In this paper, our main focus is on stock time series pattern matching, while both the whole time series and subsequence matching will be discussed. The paper is divided into five sections. Section 2 contains a discussion of related works. The proposed stock time series patternmatching schemes is introduced in Section 3. The simulation results are reported in Section 4 and the conclusion will be in the final section.

2. Related works

A simple method to deal with pattern matching between series is to compute the point-to-point distance so that the average error among the data points in the sequences can be measured. For mean-squared error distance measure, the distance between sequences $P = (p_1, ..., p_m)$ and $Q = (q_1, ..., q_m)$ is computed as

$$Dist(P,Q) = \frac{1}{m} \sum_{k=1}^{m} (p_k - q_k)^2.$$
 (1)

The main problem of point-to-point distance measure is that the number of data points in the sequences has to be the same, which cannot be satisfied by most applications. A direct solution is to compress the longer time series by evenly dividing it into segments of the same number as the data points in the shorter time series and use the mean of data points in each segment to represent the whole segment. Mathematically, for sequences $P = (p_1, ..., p_m)$ and $Q = (q_1, ..., q_n)$ where $n \leq m$, the distance measure is

Dist
$$(P, Q) = \frac{1}{n} \sum_{k=1}^{n} \left[\left(\frac{1}{e_k - s_k + 1} \sum_{i=s_k}^{e_k} p_i \right) - q_k \right]^2,$$
 (2)

where s_k and e_k , respectively denote the starting and ending data points of the *k*th segment in the longer sequence *P* (Yi and Faloutsos, 2000; Keogh and Pazzani, 2000) and this method is called piecewise aggregate approximation (PAA) in (Keogh and Pazzani, 2000). However, this method may not capture the general shape (structure) of the sequence after the compression of the longer sequence due to the potential of smoothing out the critical (perceptual important) points.

Therefore, devising an appropriate similarity function is by no means trivial. While the statistical literature on time series analysis is vast, it has not addressed the similarity notions that are applicable to specific domain directly. For example, stock analysis. Recent works in time series pattern matching can be categorized into two general approaches. The first approach maps time sequences into other domains while the second one processes the time sequences directly in time domain. The transformation approach, pioneered by Faloutsos et al. (1994), in general computes a discrete Fourier transform (DFT) for each sequence and selects the first few coefficients to index their respective original sequences. Sequences with matching coefficients are considered similar. While the focus of Faloutsos et al. (1994) is on whole sequence matching, the work of Agrawal et al. (1993) allows subsequence matching. A framework based on wavelet decomposition is presented by Struzik and Siebes (1998). Chan and Fu (1999) applied discrete wavelet transform (DWT) for time series pattern matching. For the time domain approach, Keogh and Smyth (1997) proposed a probabilistic model based on linear segmentation of time sequence in accordance with prior knowledge for efficient representation. Xia (1997) proposed methods for efficient retrieval of all the series in the time series dataset with a shape similar to a search template (in time domain).

Fast similarity searching in large time sequences typically adopts ED as a dissimilarity measure. It is required to permit local accelerations and decelerations in the rate of sequences, leading to a popular, field-tested dissimilarity measure called the "time warping" distance. Based on the dynamic time warping (DTW) technique, the proposed method predefines some patterns to serve as templates for the purpose of pattern detection (Berndt and Clifford, 1994).

In this paper, we proposed two time series patternmatching approaches: template- and rule-based approaches. The pattern-matching methods focus on time domain integrating the prior knowledge intuitively and are relatively suitable in financial time series analysis literature (i.e. technical analysis). In the next section, our proposed stock time series pattern-matching methods will be described in detail.

3. Stock time series pattern matching

The proposed scheme adopts the time domain approach, which is more intuitive and understandable to stock market analysts and investors. Time series pattern matching based on perceptually important point (PIP) identification is first introduced by Chung et al. (2001). As to the technical analysis of stock data, the frequently used stock patterns are typically characterized by a few critical points. For example, the head-and-shoulder pattern should at least consist of a head point, two shoulder points and a pair of neck points. These points are perceptually important in the human identification process and should also be taken into accounts in the pattern-matching process. The proposed scheme follows this idea by locating those PIPs in the data sequence P in accordance with the query sequence Q. The whole time series pattern retrieval process can be divided into two phrases, i.e. PIP identification and similarity measure. Also, a controlled mechanism on the width of the matching results, instead of fixing the length, during the subsequence time series pattern-matching process will be given at the end of this section.

3.1. PIP identification

With sequences P and Q being normalized to a unit square (for shifting and uniform amplitude scaling invariant), the PIPs are located in order according to Fig. 2. Currently, the first two PIPs will be the first and last points of P. The next PIP will be the point in P with maximum distance to the first two PIPs. The fourth PIP will then be the point in P with maximum distance to its two adjacent PIPs, i.e., in between either the first and second PIPs or the second and the last PIPs. The PIP location process continues until the length of SP is equal to that of query sequence Q.

To determine the maximum distance between the two adjacent PIPs, three distance measures are proposed. As illustrated in Fig. 3a, the first measure is the sum of the EDs of the test point $p_3 = (x_3,y_3)$ to its adjacent PIPs $p_1 = (x_1,y_1)$ and $p_2 = (x_2,y_2)$, i.e.,

$$ED(p_3, p_1, p_2) = \sqrt{(x_2 - x_3)^2 + (y_2 - y_3)^2} + \sqrt{(x_1 - x_3)^2 + (y_1 - y_3)^2}.$$
(3)

This measure is biased towards the middle part of the region covered by p_1 and p_2 . The second measure is the perpendicular distance (PD) between the test point p_3 and the line connecting the two adjacent PIPs as shown in Fig. 3b, i.e.,

Slope
$$(p_1, p_2) = s = \frac{y_2 - y_1}{x_2 - y_1},$$
 (4)

$$x_c = \frac{x_3 + (sy_3) + (s^2x_2) - (sy_2)}{1 + s^2} - (x_3)^2,$$
(5)

$$y_c = (sx_c) - (sx_2) + y_2,$$
 (6)

$$PD(p_3, p_c) = \sqrt{(x_c - x_3)^2 + (y_c - y_3)^2}.$$
(7)

The final measure, depicted in Fig. 3c, is the vertical distance (VD) between the test point p_3 and the line

```
Procedure PIPIdentification (P,Q)
Input: sequence P[1..m], template Q[1..n]
Output: pattern SP[1..n]
Begin
Set SP[1]=P[1], SP[n]=P[m]
Repeat until SP[1..n] are all filled
Begin
Select point P[j] with maximum distance to the adjacent points in SP (SP[1]
and SP[n] initially)
Add P[j] to SP
End
Return SP
End
```

Fig. 2. Pseudo code of the perceptually important point identification process.



Fig. 3. Distance measure for PIP Identification: (a) Euclidean distance based: PIP-ED, (b) perpendicular distance based: PIP-PD and (c) vertical distance based: PIP-VD.



Fig. 4. Identification of 7 perceptually important points (head-and-shoulder pattern).

connecting the two adjacent PIPs, i.e.,

$$VD(p_3, p_c) = |y_c - y_3| = \left| \left(y_1 + (y_2 - y_1) \frac{x_c - x_1}{x_2 - x_1} \right) - y_3 \right|,$$
(8)

where $x_c = x_3$. It is intended to capture the fluctuation of the sequence and the highly fluctuated points would then be considered as PIPs.

To illustrate the identification process, the head-andshoulder pattern is used and Fig. 4 shows the step-by-step result from the ED measure. Here, the number of data points in the input sequence P and query sequence Qare 29 and 7, respectively, i.e., m = 29 and n = 7. By using the perpendicular and VD measures, the same set of PIPs can be identified but the order in locating the fifth and sixth points, corresponding to the lower right two figure blocks, is interchanged. In both cases, the located PIPs correspond pretty well to the shape of the head-and-shoulder pattern.

After identifying the PIPs of the subsequence, a similarity measuring mechanism is essential for pattern matching. Two different approaches are introduced in the following subsections.

3.2. Template-based pattern-matching approach

The direct way to achieve the goal of similarity measure is template matching. By defining the shape of the query patterns (pattern templates) visually, point-topoint direct comparisons can be carried out. We termed this process as the template-based approach. Together with PIP identification, it was first introduced by Chung et al. (2001). Fig. 5 shows a set of typical reversal technical analysis pattern templates with lengths equal to 7 PIPs.



Fig. 5. Five typical technical analysis reversal patterns.

As different sequences may have different "amplitudes", after identifying the PIPs in the data sequence, it is necessary to re-scale the points so that the comparison between sequences in different "amplitudes" range (e.g. 0-1) can be facilitated. This is typically addressed as normalizing all the sequence values to a given range. Then, the amplitude distance (AD) between P and Q can be computed by using point-to-point direct comparison, i.e.,

$$AD(SP, Q) = \sqrt{\frac{1}{n} \sum_{k=1}^{n} (sp_k - q_k)^2}.$$
(9)

Here, SP and sp_k denote the PIPs found in P. However, the measure in Eq. (9) has not yet taken the horizontal scale (time dimension) into considerations. Therefore, it is preferred to consider the horizontal distortion of the pattern against the pattern templates. The temporal distance (TD) between P and Q is defined as

$$TD(SP, Q) = \sqrt{\frac{1}{n-1} \sum_{k=2}^{n} (sp_k^t - q_k^t)^2},$$
(10)

where sp_k^t and q_k^t denote the time coordinate of the sequence points sp_k and q_k , respectively. To take both horizontal and vertical distortion into consideration in our similarity measure, the distance (or similarity) measure could be modified as

$$D(SP, Q) = w_1 \times AD(SP, Q) + (1 - w_1) \times TD(SP, Q),$$
(11)

where w_1 denotes the weighing among the AD and TD and can be specified by the users. In our previous experiments, a reasonable setting of w_1 is 0.5 and this figure will be adapted in all the experiments of this paper.

3.3. Rule-based pattern-matching approach

Besides defining the preferred patterns visually as pattern templates, rules can be defined to describe the shape of the preferred patterns. One of the advantages of applying rulebased pattern matching over the template-based approach is that the relationship between the points is hard to define explicitly in the template-based approach. For example, in a head-and-shoulder pattern, the two shoulders in the pattern must guarantee that it is lower than the head while the two shoulders must have a similar degree of amplitude (within 15% in average). In such a case, although we can plot a pattern template according to these requirements, such kind of rules cannot be guaranteed during the pattern-matching process. Patterns with similar shape compare to the query pattern but violated rules may still be identified. Therefore, the rule-based approach gives another direction for the users to define their preferred query pattern.

Based on the definitions of technical patterns by Lo et al. (2000), we described the five reversal technical patterns, which were already shown in a previous subsection, in rule format. According to the template-based approach, it is assumed that 7 PIPs, from sp_1 to sp_7 , will be identified first for the pattern matching process. Therefore, the rules for describing the relationships and constraints among these 7 PIPs are defined. The corresponding definitions of the five commonly used reversal technical patterns in Fig. 5 are as following:

Rule set 1 (head-and-shoulder)

- $sp_4 > sp_2$ and sp_6
- $sp_2 > sp_1$ and sp_3
- $sp_6 > sp_5$ and sp_7
- $sp_3 > sp_1$
- $sp_5 > sp_7$
- diff(sp_2, sp_6) < 15%
- diff $(sp_3, sp_5) < 15\%$

Rule set 2 (rounded top)

- sp_3 and $sp_4 > sp_2$
- sp_4 and $sp_5 > sp_6$
- $sp_2 > sp_1$ with 75%
- $sp_6 > sp_7$ with 75% \uparrow

Rule set 3 (spike top)

- sp_1 and sp_2 and $sp_3 < sp_4$ with 75% \uparrow
- sp_5 and sp_6 and $sp_7 < sp_4$ with 75% \uparrow

Rule set 4 (double top)

- diff $(sp_3, sp_5) < 15\%$
- $sp_3 > sp_2$ and sp_4
- $sp_2 > sp_1$
- $sp_5 > sp_4$ and sp_6
- $sp_6 > sp_7$

Rule set 5 (triple top)

- diff $(sp_2, sp_4, sp_6) < 15\%$
- diff $(sp_3, sp_5) < 15\%$
- $sp_2 > sp_1$ and sp_3
- $sp_4 > sp_3$ and sp_5
- $sp_6 > sp_5$ and sp_7

where diff (sp_x, sp_y) denotes the difference between data points sp_x and sp_y , " sp_x and $sp_y > sp_z$ " denotes that sp_z must be smaller than sp_x and sp_y , " $sp_x > sp_y$ with z% \" specifies that sp_x must be greater than sp_y with z%.

With the defined rules, the sequences can then be evaluated. First, the given number of PIPs (i.e. 7 in this case) are identified from the sequences. Then, those sequences which can validate all the rules from a given query pattern are identified as a matching result.

3.4. Dynamic subsequence matching in time series

Direct time series comparison can be applied if it is focused on whole matching. For subsequence matching, it requires searching a specified pattern template within a time series using a sliding window with a fixed window size w. However, the pattern may appear in a different resolutions rather than a fixed window size w. To find all similar patterns within a time series, w must vary from 2 to the length the time series m and the number of subsequence needs to search becomes (m(m-1))/2. The similarity measure between each subsequence and the query pattern can then be calculated by the proposed time series patternmatching approaches.

From the above definition, either a given window size w must be presented or searched for all resolutions for time series subsequence searching. However, unlike traditional

database queries, which seek for data that exactly matches the given query exactly, subsequences that only slightly differ in length from the given query sequence should be allowed. For example, when a financial analyst querying using Q1, subsequences with 6–8 trading days may be the reasonable results but not only limited to 7 trading days. On the other hand, it is also not possible to create a huge pattern space with all subsequences formed in a time series (e.g., the co-existence of long-term and short-term subsequences). Therefore, the introduction of a dynamic but controllable subsequence searching technique is preferred.

To allow the searching of subsequences that are slightly different from the preferable subsequence length (resolution), a mechanism that can control the length of the subsequences towards the length specified by the users during the searching process is preferred. To achieve this goal, a temporal control penalty function is proposed and defined as follows:

$$TC(SP) = 1 - \exp^{-(d_1/\theta_1)^2},$$
 (12)

where $d_1 = \text{slen}-\text{dlen}$, that is, the difference between subsequence length (slen) and the desired subsequence length (dlen) specified by the users. The parameter θ_1 is used to control the sharpness of the function, hence the strength of the temporal control. It is defined as follows:

$$\theta_1 = dlen/dlc,$$
 (13)

where dlc is the desired length control parameter. Larger dlc values will lead to smaller θ_1 values and this will strengthen the temporal control (i.e., a shorter distance between a subsequence length and the desired length is greatly preferred).

For example, if the desired subsequence length dlen is 180 (e.g., 180 trading days) and dlc is set to 2, then $\theta_1 = 90$, and the temporal control penalty function will look like Fig. 6a. However, if dlc is set to 6 ($\theta_1 = 30$), the temporal



Fig. 6. Temporal control penalty function (dlen = 180).

control is strengthened (see Fig. 6b) by adding a greater penalty to the similarity measure for patterns with a length different from the desired one.

By defining the penalty function, only the lengths of the subsequence that fulfill the requirement (i.e. below a certain level of penalty score) are needed to evaluate. On the other hand, the subsequences that are very similar to the query pattern but with a longer or shorter length (compared to the preferred length defined by the user) can still be retrieved given that their penalty scores are within an acceptable level.

4. Experiment results

In this section, we empirically demonstrate the performance of the proposed methods. We have adopted five

```
Uniform Time Scaling
uniform time scaling of the pattern templates from P[1..n] to P[1..m], where n=7
and m=25, 43 and 61
Time Warping
If (warp) Then
  For Each critical point p[i] in P
    Move p[i] between p[previous critical point] and p[next critical point]
    randomly
  End For
End If
Noise Adding
For Each data point p[i] in P
  If randomly generated probability < a
  Then
    diff = p[i] * (random_value between 0 to b);
    p[i] = p[i] \pm diff;
  End If
End For
```

Fig. 7. Pseudo code of generating the time series pattern variants.



Fig. 8. Sample synthetic time series: head-and-shoulder (H&S), double top, triple top, rounded top and spike top (from left to right).



Fig. 9. Sample real technical patterns identified from the subsequences of stock time series: (a) head-and-shoulder, (b) double tops and (c) rounded top.



Fig. 10. Processing time with different numbers of PIP identified.



Fig. 11. Accuracy of retrieval by different PIP identification methods.



Fig. 12. Accuracy of retrieval for the synthetic dataset.

commonly used technical patterns as the query patterns and for synthetic sequence generations in our experiments. As shown in Fig. 5, they are of scale equal to seven sample points, i.e., n = 7. In the first experiment, the performance of different PIP identification methods (i.e. ED, PD and VD) is tested. Then, we simulated two sets of experiments, based on synthetic and real-time series, respectively, to compare the accuracy of the proposed template- and rulebased approaches. Accuracy here is defined as the percentage of the number of correct series retrieved from the dataset by retrieving a given number of series when a query pattern is given (i.e. the five technical patterns are used to serve as the query pattern in the experiments). That is

 $Accuracy = \frac{number of correctly retrieved series}{total number of relevant series in the dataset}.$ (14)



Fig. 13. PIP identified by the proposed approach on the sample head-and-shoulder patterns.

Pattern matching using PAA (Keogh and Pazzani, 2000) is adopted as the benchmarking method. The effect of fine-tuning the rules is evaluated afterwards. Finally, the result of subsequence pattern matching by using the template- and rule-based pattern-matching approaches is shown.

4.1. Datasets

For the synthetic time series dataset, it consists of 135 time series with different lengths, which includes 25, 43 and 61. Each of them belongs to one of the five technical patterns, head-and-shoulder, double tops,







Fig. 14. PAA result on the sample head-and-shoulder patterns.

triple tops, rounded top and spike top (Fig. 5). Each technical pattern is generated to 27 variants by applying different levels of scaling, time wrapping and noise.

First, the patterns are uniform time scaling from 7 data points to 25, 43 and 61 data points. Then, each critical point of the patterns can be warped between its previous and next critical points. Finally, noise is added to the set of patterns. The increase of noise is controlled by two parameters, namely, the probability of adding noise for each data point α and the level of noise being added to such point β . The pseudo code of the aforementioned variant generation process is shown in Fig. 7. Sample synthetic time series are shown in Fig. 8.

For the real dataset, 50 stock time series subsequences were identified by human. Each subsequence is labeled by one of the five technical patterns. Their lengths are between



Fig. 15. PIP identified by the proposed approach on the sample spike top patterns.

22 and 592 and the average length is 94. Fig. 9 shows three real technical pattern samples selected from the subsequences of stock time series.

4.2. Performance of different PIP identification methods

First, the efficiency and effectiveness of different PIP identification methods including the measurement of the VD, the PD and the ED are compared. The pointto-point similarity measure is then applied. To evaluate the efficiency, the Hong Kong Hang Seng Index (HSI) series with 2532 data points is used. Fig. 10 plots the time needed to identify different numbers of PIP. Measuring the VD is the fastest method. Measuring the PD is double in speed of VD while measuring the ED is triple in speed of VD.





Fig. 16. PAA result on the sample spike top patterns.



Fig. 17. Accuracy of retrieval for the real dataset.



Fig. 18. Accuracy of retrieval (50 out of 135) for different technical patterns.



Fig. 19. Accuracy of rule tuning.

To evaluate the effectiveness of different PIP identification methods, they are tested on the accuracy of retrieving the synthetic dataset. As shown in Fig. 11, PD has the highest accuracy among all the numbers of series retrieved. The accuracy of VD is closed to that of PD, the difference of the accuracy between VD and PD is less than 0.04. ED has the worst performance compared to that of the PD and the ED. By considering both efficiency and effectiveness, VD is the best choice for the PIP identification process and it will be adopted in the remaining experiments.

4.3. Whole sequence matching

In this section, the accuracy of using different methods to retrieve different numbers of time series from the synthetic dataset for measuring the similarity are compared. The proposed template- and rule-based approaches after the PIP identification process will be tested. VD is used in the PIP identification process. Also, w_1 is set to 0.5 for the template-based approach. The proposed approaches are benchmarked with a popular time series pattern-matching method: PAA. By using PAA, the dimension of the time series will be reduced to the same as the minimum length of the time series in the dataset (i.e. 25 in this experiment). Fig. 12 shows the average accuracy of the pattern-matching approaches on the synthetic dataset. The proposed approaches outperformed the traditional pattern-matching method (PAA) especially when the number of series retrieved is small. The PIP identification-based methods have outstanding



Fig. 20. Precision of rule tuning.



Fig. 21. Comparison the speed for subsequence searching between template-based and rule-based approaches.

performance in the technical pattern-matching process because these approaches compare the overall shape of the series instead of using point-to-point comparison. When matching the technical pattern, the similarity of the outlook of the pattern is much more important than the point-to-point distance of all the data points in the series, especially when the shape of the pattern is warped.

Then, the visualization effect of each approach is evaluated in detail. First, Fig. 13 shows the sample results of the PIP identification process for capturing the shape of the head-and-shoulder pattern. As shown in the figure, all the three patterns, which the shape were warped and noise was added, the seven correct PIPs were identified and a head-and-shoulder shape was captured in the matching process. However, the shape of the head-and-shoulder can only be retained in the first sample when using PAA (Fig. 14a). Smoothing effect can be seen in the second and third samples (Fig. 14b and c) which the original shape of the patterns are warped. Similar result can be seen in the spike top samples as shown in Figs. 15 and 16. By using the PIP approach, the shape of the spike top pattern can be captured even the pattern is warped (Fig. 15b and c) while the PAA smoothed out the spike top when the shape of the pattern is distorted (Fig. 16b and c). To sum up, the performance of PAA is worse than the two methods based on PIPs especially when the number of retrieved series is small. The problem of PAA is due to its mechanism will smooth out the critical points of the series.

On the other hand, the accuracy of the rule-based method kept constant in Fig. 12. It is because the rulebased method will only be determined if a series fulfils the criteria set by the rules during the matching process. Therefore, the number of series retrieved would not affect the accuracy. Instead, the way to increase the accuracy of the rule-based approach is fine-tuning the rules.

A similar result is obtained by applying the three pattern-matching approaches on the real dataset as shown in Fig. 17. The proposed template-based approach outperformed the benchmarking approach. However, the performance of the rule-based approach is worse than the PAA this time. It is because the patterns from the stock time series identified by human are subjective and the variation is much higher. Therefore, these time series patterns are much harder to fulfill the criteria of the rules. As we can see, the overall performance on the real dataset is worse than that of the synthetic dataset.

In the last experiment of this subsection, the characteristics of different pattern-matching approaches on the five technical patterns were studied. The synthetic dataset was used. As shown in Fig. 18, the template-based approach worked well on the head-and-shoulder, rounded top, triple tops and spike top patterns. However, they were weak at identifying the rounded top pattern as it is hard to identify the PIPs in a rounded top pattern. A rounded top pattern is difficult to characterize by the criteria points. Moreover, the result shows the strength of the rule-based approach. It can distinguish the head-and-shoulder, triple tops and double tops patterns successfully which is a difficult task for the template-based and PAA approaches.

4.4. Rule tuning

For the rule-based pattern-matching approach, as the time series will either fulfill or not fulfill the criteria of the



Fig. 22. Identification of a "Triple Top" pattern using different approaches (a) PAA, (b) template-based and (c) rule-based (dlen = 90).



Fig. 23. Zoom-in of the subsequence identified by rule-based approach in Fig. 22 (c) (i.e. "Triple Top" pattern).

rules, the number of query result will not affect the accuracy. In this subsection, the accuracy and the precision are adopted to measure the performance of the rule-based matching approach. Precision is defined as the percentage of correct pattern among the time series that fulfilled the criteria of the rules for describing a query pattern. The synthetic dataset is used to evaluate the effect of tuning the rules. The acceptance range in the rules varies from -10% to 10% to evaluate the effect. For example, the acceptance of the differences between the data points in the head-and-shoulder pattern (i.e. rules: diff(*sp*₂, *sp*₆) < 15% and diff(*sp*₃, *sp*₅) < 15%) are adjusted to 5%, 10%, 15% (original), 20% and 25%.

Figs. 19 and 20 show the accuracy and precision. By tuning the rules, the accuracy for each query pattern is adjusted, except the rounded top pattern. By relaxing the rules, the number of correct patterns retrieved increased. However, the number of wrong patterns retrieved is also increased. As a result, the precision is almost unchanged, except that when the acceptance range of the spike top pattern is adjusted to +10%. The number of match patterns becomes zero. In conclusion, the tightening or relaxing of the rules depends on the usage of the analysts.

4.5. Subsequence matching in stock time series

In the last experiment, the subsequence pattern matching result based on the proposed approaches is shown. Again, PAA is adopted as the benchmark. The five commonly used reversal technical analysis patterns, as shown in Fig. 5, were used in testing the template-based patternmatching approach, while the definitions in Section 3.3 were used for the rule-based approach as the query patterns. The past 10 years Hong Kong HSI time series is used (2532 data points) for the identification of different query patterns defined. First, the processing time for subsequence searching is compared in Fig. 21. Similar time was needed for subsequence searching in the two proposed approaches. However, in the rule-based approach, there was a great variation in speed among different patterns. It depends on the number of rules needed to be verified. On the other hand, the speed was nearly the same among different patterns by using the template-based approach because the distance is calculated based on the same number of data points.

From the visualization results (Figs. 22–26), in general, the PAA approach has more mismatched subsequences. The template-based approach provides more accurate results. However, wrong identification is still appeared and the query results cannot fulfill the criteria of the query pattern, which is important in technical analysis in the financial domain. In Fig. 22, we tried to identify the triple tops pattern with length = 90 but some of the identified subsequences by template-based approach (Fig. 22b) (also by PAA approach (Fig. 22a)) were more like a head-andshoulder pattern. It is because the shape of the triple tops and the head-and-shoulder patterns are similar in outlook when represented by the query patterns. In such a case, the rule-based approach can facilitate to specify the constraints



Fig. 24. Identification of a "Spike Top" pattern using different approaches (a) PAA, (b) template-based and (c) rule-based (dlen = 180).

and rules can be used for describing the shape of the query pattern and the relationship among the data points in the pattern. Therefore, the rule-based approach is more effective in distinguishing such kinds of pattern template. As we can see, all the head-and-shoulder-like subsequences were filtered using the rule-based approach during the searching of triple tops patterns and another view of



Fig. 25. Zoom-in of the subsequence identified by rule-based PIP approach in Fig. 24(c) (i.e. "Spike Top" pattern).

subsequence is identified in Fig. 22c (zoom-in is shown in Fig. 23).

Furthermore, depending on the complexity and constrains of the rules defined, less subsequences can fulfill the rules when more constraints are applied such as the case in this experiment. Fig. 24 shows an example with similar behavior that head-and-shoulder-like patterns were obtained when querying a spike top pattern in dlen = 180 with the template-based approach (Fig. 24b). However, there is no such problem in the rule-based approach (Fig. 24c, zoom-in of the subsequence is shown in Fig. 25). Fig. 26 shows another example for searching head-andshoulder subsequences with dlen = 360.

5. Conclusion

In this paper, two flexible time series pattern-matching approaches, template- and rule-based approaches, based on perceptually important points are introduced for time series pattern searching. They follow the time domain approach to carry out the matching process and are intuitive to ordinary data analysts. One may find it particularly attractive in applications like stock data analysis. The proposed approaches are efficient and also effective. As demonstrated in the experiments, the template-based approach provides an effective time series pattern matching tool, while the rule-based approach provides further ability for describing the query patterns and is constrainable on the shape of the query patterns. Future work includes developing a hybrid pattern-matching algorithm based on both the template- and rule-based approaches to obtain their advantages. That is, using a template-based approach to obtain its visualization flexibility, while the rule-based approach is used to specify the necessary requirements and constraints of the query pattern. Moreover, the importance of the data points (the identification order of the PIPs) can be taken into account during the similarity measure.



Fig. 26. Identification of a "head and shoulders" pattern using different approaches (a) PAA, (b) template-based and (c) rule-based (dlen = 360).

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